

Homework #4

Chapter 21

1. McQuarrie and Simon Problems: 4,5,12,14,40,43
2. a) Given the partition function of a diatomic gas:

$$q(V, T) = \left(\frac{2\pi M k_B T}{h^2} \right)^{3/2} V \frac{T}{\sigma \Theta_{rot}} \frac{e^{-\Theta_{vib}/2T}}{1 - e^{-\Theta_{vib}/T}} g_e e^{D_e/k_B T} \quad \text{where } Q(N, V, T) = \frac{q^N}{N!}$$

find an equation for the standard molar entropy.

- b) Use your answer from part 2a) and the data in Chapter 18 to calculate the standard molar entropy of CO(g) at its standard boiling point, 81.6 K.
- c) Compare your answer from part 2b) with the experimental value of $155.6 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$. Why is there a discrepancy of about $5 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$?

Chapter 22

1. The molar enthalpy of vaporization of benzene at its normal boiling points (80.09°C) is 30.72 kJ/mol . Assuming that $\Delta_{vap}\bar{H}$ and $\Delta_{vap}\bar{S}$ are temperature independent, calculate the value of $\Delta_{vap}\bar{G}$ at 75°C , 80.09°C , and 85.0°C . Explain your results.
2. Use the van der Waals equation to derive an expression for $\bar{U}(T, \bar{V}) - \bar{U}^{id}(T, \bar{V})$. Use your result along with the van der Waals equation to calculate the value of $\bar{U}(T, \bar{V})$ for ethane at 400 K given that $\bar{U}^{id}(T, \bar{V}) = 14.55 \text{ kJ/mol}$. (Display results graphically like Fig 22-3). To do this, use a range of \bar{V} of 0.0700 L/mol to 7.00 L/mol and calculate both $\bar{U}(T, \bar{V})$ and $P(T, \bar{V})$.
3. Determine $\bar{C}_p - \bar{C}_v$ for a gas that obeys the equation:
 - a. $P(\bar{V} - b) = RT$
 - b. $PV = nRT$
4. What are the natural variables of the entropy? Explain your answer briefly.
5. Starting from $dU = TdS - PdV$ derive the Maxwell equation below:

$$\left(\frac{\partial T}{\partial V} \right)_S = - \left(\frac{\partial P}{\partial S} \right)_V$$

6. How much energy is available for sustaining muscular and nervous activity from the combustion of 1.00 mol of glucose molecules under standard conditions at 37°C (i.e., blood temperature)? The standard entropy of reaction is $182.4 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$. [Hint: Find other necessary values on NIST.] How is this related to the maximum non-PV work?
7. Calculate $\Delta_r G(375\text{K})$ for the reaction $2\text{CO}(g) + \text{O}_2(g) \rightarrow 2\text{CO}_2(g)$ from the appropriate values of $\Delta_r G(298\text{K})$, $\Delta_r H(298\text{K})$, and the Gibbs-Helmholtz equation. [Again, you may need to use NIST or another thermodynamic table.]
8. When 2 moles of gas at 330 K and 3.50 atm is subjected to isothermal compression, the entropy drops by 25.0 J/K . Find the final pressure and the Gibbs free energy.

9. For each of the following processes, state which of the quantities ΔU , ΔH , ΔS , ΔA , and ΔG are equal to zero:
- Isothermal reversible expansion of an ideal gas
 - Adiabatic reversible expansion of a non-ideal gas
 - Vaporization of liquid water at 80 °C and 1 bar pressure.
 - Vaporization of liquid water at 100 °C and 1 bar pressure.
 - Reaction between H_2 and O_2 in a thermally insulated bomb.

For Presentation (Oct 26):

Group J: Chapter 21, M&S #14

Group A: Chapter 22, #2

Note to Group B: You'll be presenting on the next set of homework, not this one.