

Assignment #3

Recommended Problems (not to be handed in)

All of these problems are from McQuarrie & Simon.

D-4, D-6, D-8; 5-37, 5-28; 13-20, I-3, I-13

Required Problems (Due March 16 at 3 pm)

You will want/need to use Excel or other plotting program for some of these problems.

1. McQuarrie & Simon: D-2, D-7, D-12; 5-33, 5-35; 13-16, 13-33, 13-34, 13-35, 13-36

2. a) Show that $\sigma_x = \langle x^2 \rangle^{1/2}$ for the harmonic oscillator. When this relationship is true, the standard deviation is often called the root-mean-square-displacement.
- b) Find the expressions of $\langle \psi_v | x^2 | \psi_v \rangle$ for the first two states of the harmonic oscillator. (Note the use of Dirac notation.) See Problem 5-20 if you get stuck.
- c) Using the fundamental vibrational frequencies given in Table 1, calculate the root-mean-square-displacement for each molecule in the $v=0$ state and compare the magnitude of the root-mean-square-displacement to the equilibrium bond lengths, R_e .

Table 1: Info for Problem #2

| Molecule | $\tilde{\nu} / \text{cm}^{-1}$ | R_e / pm |
|-----------------------------------|--------------------------------|-------------------|
| H ₂ | 4401 | 74.1 |
| ³⁵ Cl ³⁵ Cl | 554 | 198.8 |
| ¹⁴ N ¹⁴ N | 2330 | 109.4 |

3. The Morse potential is an analytical expression which more accurately models the internuclear potential than the harmonic oscillator model. (See Example 5-2 for more on the Morse potential.) A Maclaurin expansion of the Morse potential yields:

$$V(x) = D\beta^2 x^2 + \dots$$

Given that $D = 8.19 \times 10^{-19} \text{ J/molecule}$, $\tilde{\nu}_e = 1580.0 \text{ cm}^{-1}$, and $R_e = 121 \text{ pm}$ for ¹⁶O₂, calculate the force constant of ¹⁶O₂. Plot the Morse potential for ¹⁶O₂ and the corresponding harmonic oscillator potential on the same graph. (It should look like Figure 5.5).

4. Given the following parameters for ¹²C¹⁶O: $\tilde{T}_e = 6.508043 \times 10^4 \text{ cm}^{-1}$, $\tilde{\nu}_e' = 1514.10 \text{ cm}^{-1}$, $\tilde{x}_e' \tilde{\nu}_e' = 17.40 \text{ cm}^{-1}$, $\tilde{\nu}_e'' = 2169.81 \text{ cm}^{-1}$, and $\tilde{x}_e'' \tilde{\nu}_e'' = 13.29 \text{ cm}^{-1}$, make a table of the first four vibrational states in the first two electronic states. In addition, determine the allowed transitions from $v'' = 0$ (put these values in a second table).
5. Calculate the moment of inertia and rotational constant, B, of H₂O around its twofold axis of symmetry (the bisector of the HOH angle). The bond angle is 104.5° and each bond length is 95.7 pm. Recall $I = \sum m_i r_i^2$ where m_i is the mass of each atom and r_i is the perpendicular distance from the axis of rotation.

