

- 5a:** [HKK 5.15] Write a higher-order procedure called `make-function-with-exception` that takes two numbers and a procedure as parameters and returns a procedure that has the same behavior as the procedural argument except when given a special argument. The two numerical arguments to `make-function-with-exception` specify what that exceptional argument is and what the procedure made by `make-function-with-exception` should return in that case. For example, the `usually-sqrt` procedure that follows behaves like `sqrt`, except that when given the argument 7, it returns the result 2:

```
(define usually-sqrt
  (make-function-with-exception 7 2 sqrt))
```

```
(usually-sqrt 9)
3
```

```
(usually-sqrt 16)
4
```

```
(usually-sqrt 7)
2
```

- 5b:** [HKK 5.16] If two procedures f and g are both procedures of a single argument such that the values produced by g are legal arguments to f , the *composition* of f and g is defined to be the procedure that first applies g to its argument and then applies f to the result. Write a procedure called `compose` that takes two one-argument procedures and returns the procedure that is their composition. For example, `((compose sqrt abs) -4)` should compute the square root of the absolute value of -4 .

- 5c:** [HKK 5.20] Suppose the following have been defined:

```
(define f
  (lambda (m b)
    (lambda (x) (+ (* m x) b))))
```

```
(define g (f 3 2))
```

For each of the following expressions, indicate whether an error would be signaled, the value would be a procedure, or the value would be a number. If an error is signaled, explain briefly the nature of the error. If the value is a procedure, specify how many arguments the procedure expects. If the value is a number, specify which number.

- (a) `f`
- (b) `g`
- (c) `(* (f 3 2) 7)`
- (d) `(g 6)`
- (e) `(f 6)`
- (f) `((f 4 7) 5)`

- 5d:** Write a procedure `(estimate-integral f a b)` which estimates the integral $\int_a^b f(x) dx$. (Do not panic if you have not had calculus.) One way to do this is by a Riemann sum. For example,

$$\int_2^5 f(x) dx \approx .01 \cdot [f(2.00) + f(2.01) + f(2.02) + \cdots + f(4.99)]$$

More generally,

$$\int_a^b f(x) dx \approx \delta \cdot [f(a) + f(a + \delta) + f(a + 2\delta) + f(a + 3\delta) + \cdots + f(a + n\delta)]$$

where δ is a small positive number and $a + n\delta \approx b$.

- (a) Write the procedure (`estimate-integral f a b`), fixing $\delta = .01$ as in the first example above. Refer to any calculus textbook to identify a few test cases.
- (b) Write the procedure (`estimate-integral-with-step f a b delta`) which takes the step δ as an argument.
- (c) Write a procedure (`make-integrator delta`) which takes an argument δ and returns a procedure. That procedure should accept three arguments `f`, `a`, and `b`, and estimate $\int_a^b f(x) dx$ using a Riemann sum with step δ .
- (d) Optional: Can you find functions for which this Riemann sum gives a very bad estimate? Can you improve the program to work with some of these troublesome functions?