

# MCS-236 Homework 10

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**Definition** A graph  $G$  is said to be *minimal connected* if  $G$  is connected but for any edge  $e$  of  $G$ , the graph  $G - e$  is not connected.

A graph  $G$  is said to be *maximal acyclic* if  $G$  is acyclic but for any nonadjacent vertices  $u, v$  of  $G$ , the graph  $G + uv$  contains some cycle.

1. Prove that  $G$  is a minimal connected graph if and only if  $G$  is a tree.
2. Prove that  $G$  is a maximal acyclic graph if and only if  $G$  is a tree.